
I Want To Be a Computational Mathematician

(with apologies to Paul Halmos)

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Science in the 1890's

Experimental Science

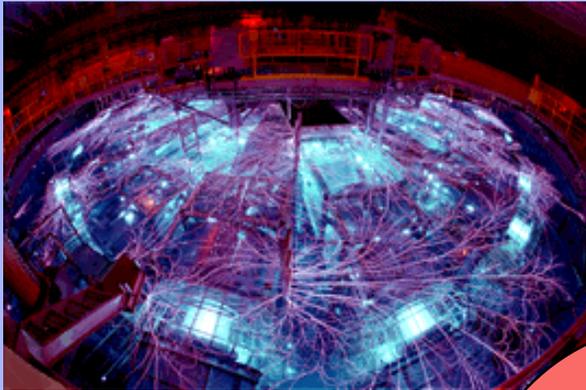


Theoretical Science



Science in the 1990's

**Experimental
Science**



**Theoretical
Science**



Computational Science



Modeling and simulation are being used in safety critical situations



<http://www.boeing.com/commercial/777family>

- ❖ The Boeing 777 is the first jetliner to be 100 percent digitally designed using three-dimensional solids technology.
- ❖ Throughout the design process, the airplane was preassembled on the computer, eliminating the need for a costly, full-scale mock-up.

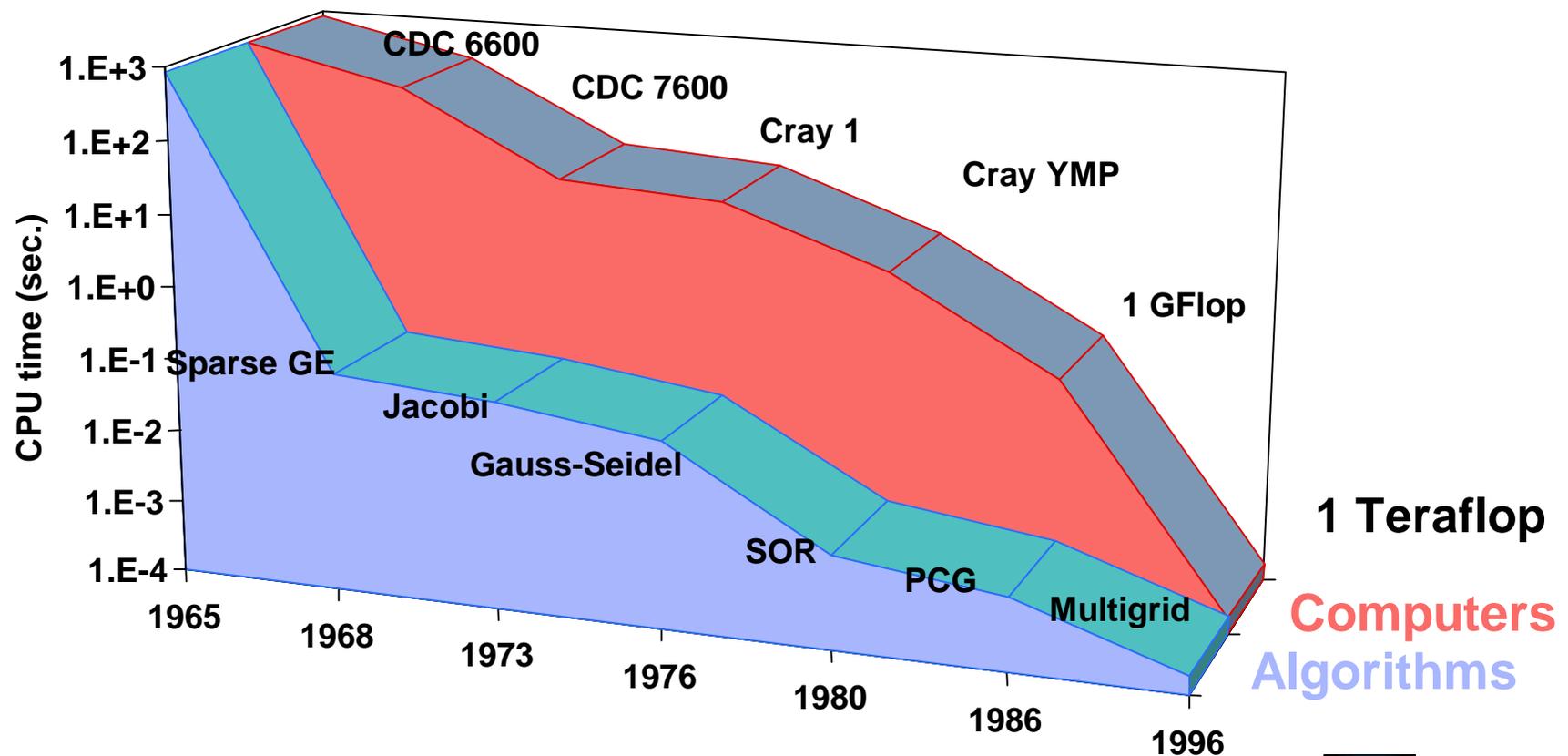
Boeing expects 20% less manufacturing errors.

What's different today from yesterday?

- ❖ Experimental science has become increasingly difficult and expensive to do
- ❖ Computing power has increased tremendously
- ❖ Computational sciences and mathematics has taken on a new role
- ❖ Improvements in algorithm development have outpaced computing improvements !!!

New algorithms have yielded greater reductions in solution time than hardware improvements

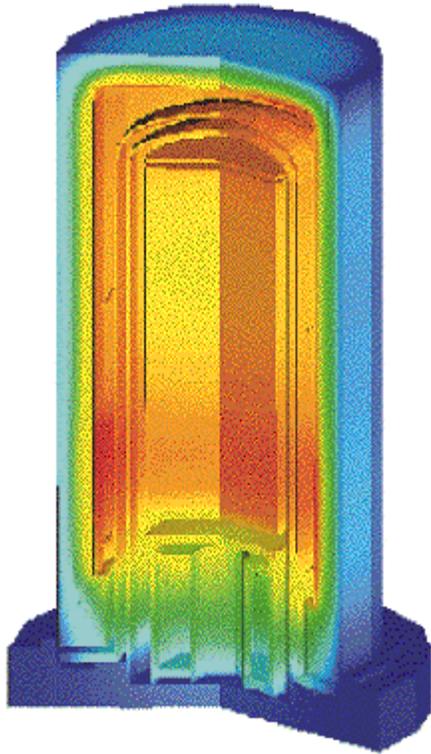
Gaussian Elimination/CDC 3600



Quick tour of projects at Sandia

- ❖ Computational mathematics at Sandia is applications driven
- ❖ I'll only touch on 2 major areas
 - ❖ optimization
 - ❖ iterative methods for linear systems
- ❖ (Many) More details can be found at
 - ❖ <http://csmr.ca.sandia.gov>
 - ❖ <http://www.cs.sandia.gov>

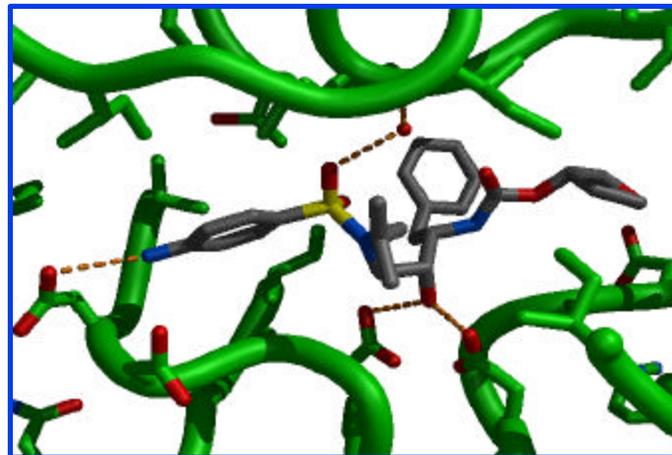
Optimization methods are used in a variety of applications



Temperature fields in a vertical, stacked-wafer, low-pressure, chemical-vapor-deposition furnace

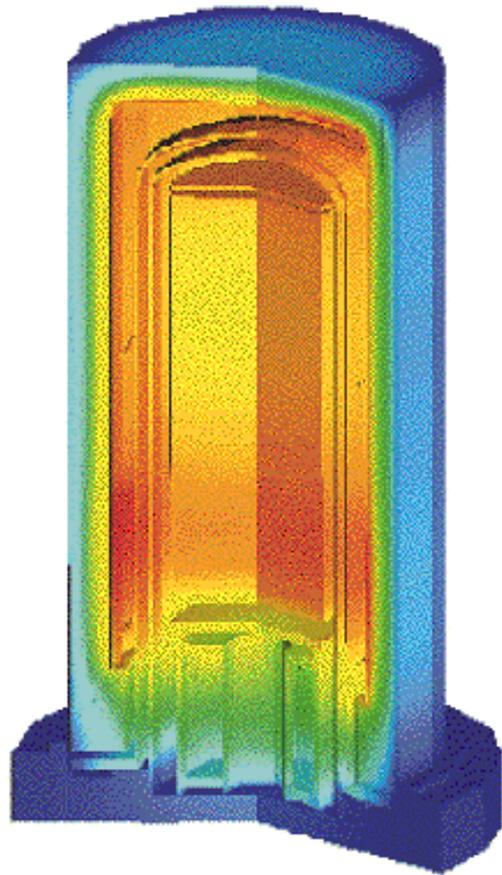


Predictive fire codes can help fight aircraft fires

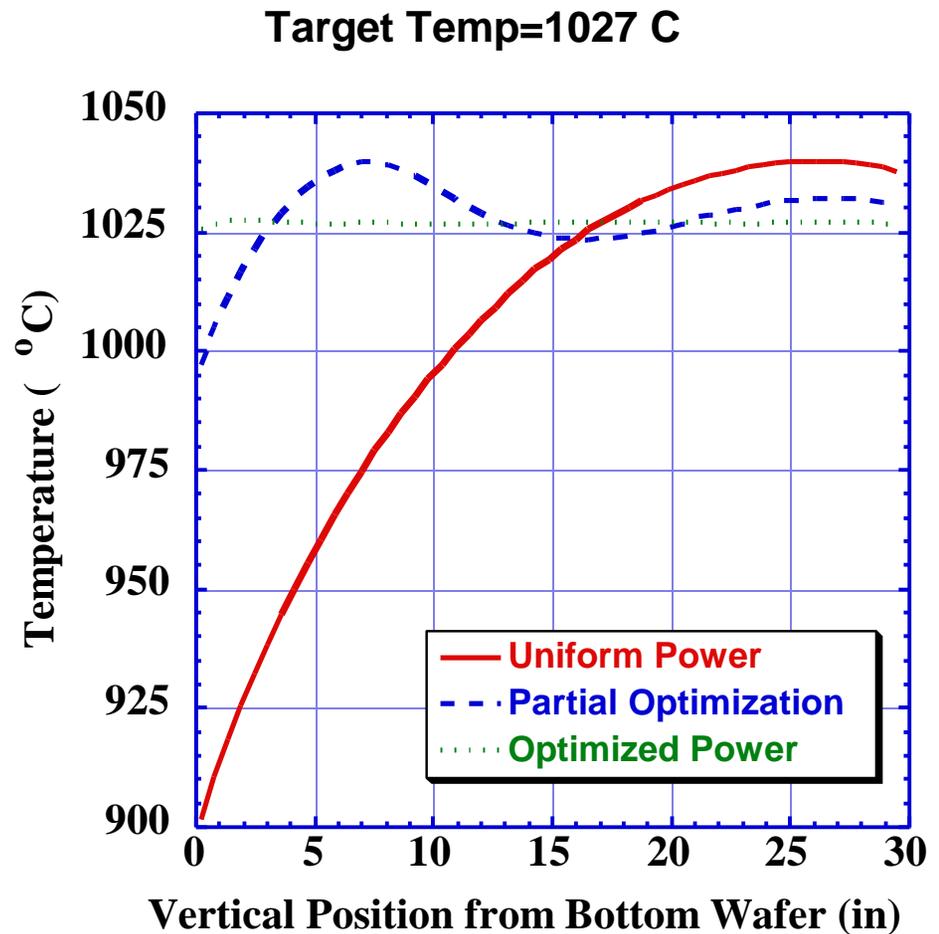


HIV-1 Protease complexed with Vertex drug VX-478

Optimized power distribution enhances wafer temperature uniformity for steady-state open-loop operation



Temperature fields in a vertical, stacked-wafer, low-pressure, chemical-vapor-deposition furnace

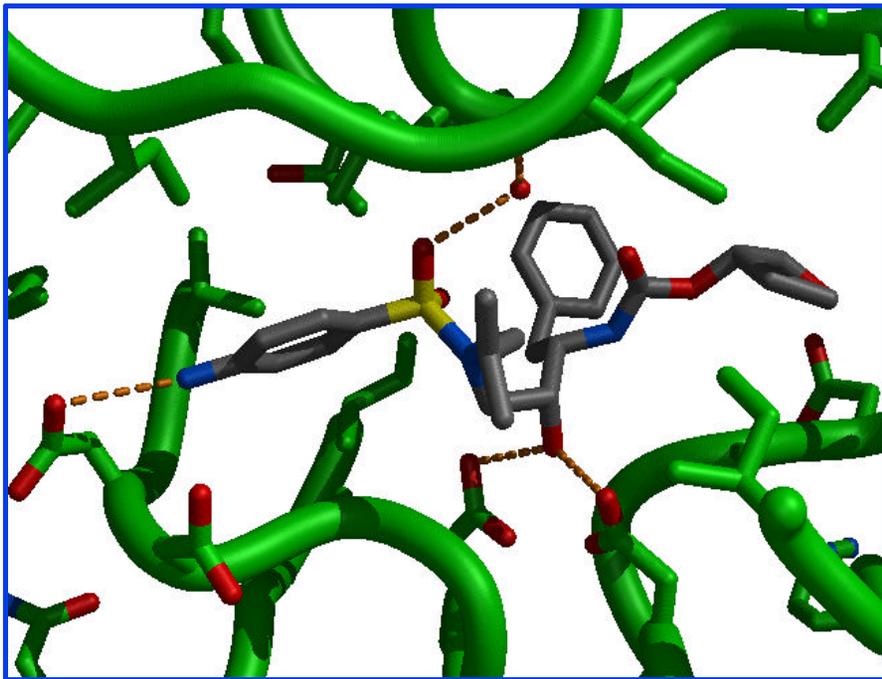


Model-based safety assessments can be used to simulate accident scenarios



- ❖ Goal is to determine the worst-case response
- ❖ Simulation of coupled sub-systems requires new methods
- ❖ Complex physics and 3D geometries make this a difficult problem

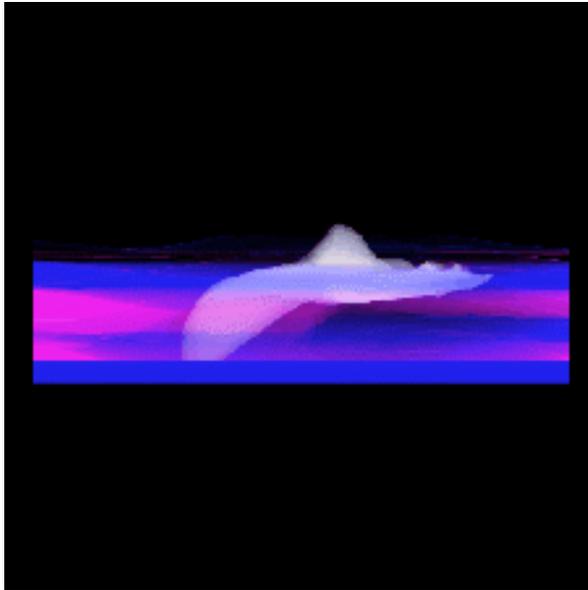
Drug design can be viewed as an energy minimization problem in computational chemistry



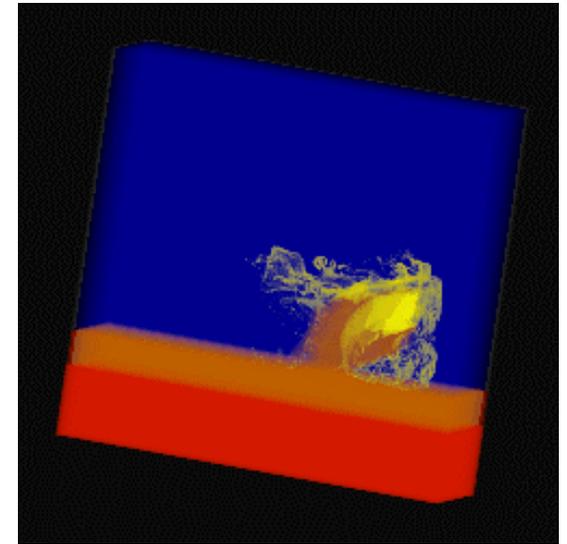
HIV-1 Protease Complexed with
Vertex drug VX-478

- ❖ A single new drug may cost over \$200 million to develop and the design process is typically takes about 13 years
- ❖ Typically there are thousands of parameters and constraints
- ❖ There are thousands of local minima

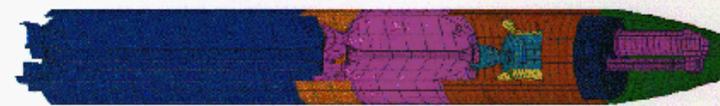
Other interesting mathematical problems arise in the solution of large linear systems of equations



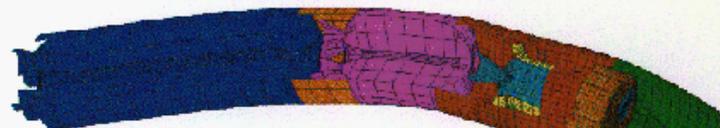
Simulation of
1 km comet
splashing into
the Atlantic
ocean using
50 M cell
calculation



Visualization of a
large oil and gas
data set (about
100 million cells).



Undeformed



First Bending Mode

Linear structural
dynamics analysis
requires MP
eigensolvers

Recap

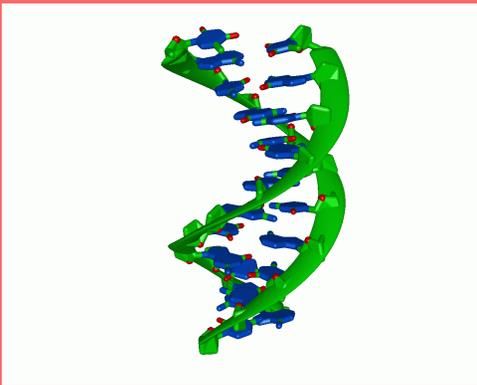
- ❖ Modeling and simulation have taken on a new role in scientific discovery
 - ❖ Many projects are in relatively new fields
 - ❖ Almost all projects are interdisciplinary
 - ❖ Solutions to these problems require intensive computational resources
- ❖ Computational mathematics is at the heart of most simulations
- ❖ New computing paradigms force us to constantly change our way of thinking

A few areas of research include:

- ❖ Basic algorithm development, especially in the area of scalable parallel algorithms
- ❖ Parallel optimization methods for large-scale nonlinear constrained problems
- ❖ Parallel linear solvers for problems with > 10 billion unknowns

Science in 2050 ?

**Computational
Science**



**Theoretical
Science**



?

Experimental Science

Where do we go from here

- ❖ We desperately need to have more people in computational mathematics
- ❖ Must have a fundamental understanding of the mathematics
- ❖ Must have a strong computing background
- ❖ Need to have new ways of thinking about problems

Why do I want to be a computational mathematician?

- ❖ Challenging problems of national importance
- ❖ Wide range and diversity of problems
- ❖ FUN !!!!